

Week 2, Challenge 2

The operation \star is defined on the set \mathbb{Q}^+ of positive rational numbers by

$$a \star b = \frac{ab}{2},$$

for positive rational numbers a and b .

Determine, with explanation, whether \mathbb{Q}^+ is a group under the operation \star .

(Note that 0 is not a positive rational number.)