

MAPPER CLUSTERING

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Output

$$K = \text{Nerve}(\{S_{\alpha,j}\}_{\alpha \in A, 1 \leq j \leq n_\alpha})$$

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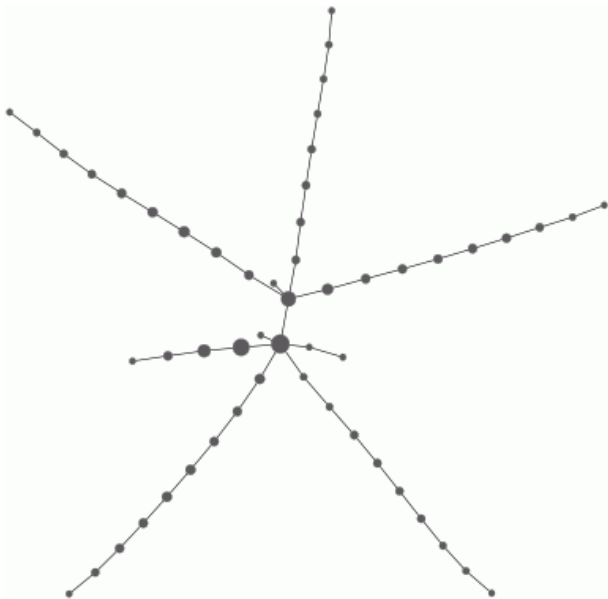
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Mapper output for starfish sample



Example 2 : $\mathbf{S} = \{\mathbf{v}_1, \dots, \mathbf{v}_{310}\} \subset \mathbf{X} \subset$ all breast tissue samples

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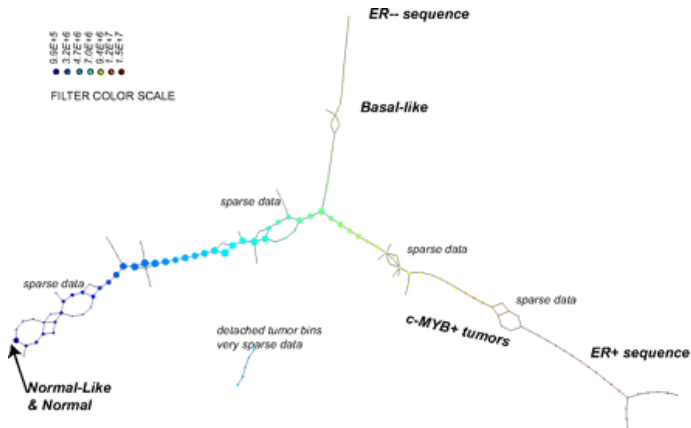
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