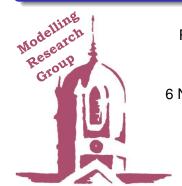


Mathematical Modelling



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### Outline

#### Last time

- Biology
- 2 Experiments
- Experimental Results
- Some Modelling Assumptions
- Modelling Uptake

#### Today:

- Compartment Model
- Parameter Estimation
- Modelling Results
- Future Work

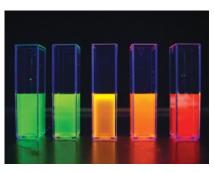


Figure: Various sizes of QDs

Gun'ko group, TCD

# Some Modelling Assumptions

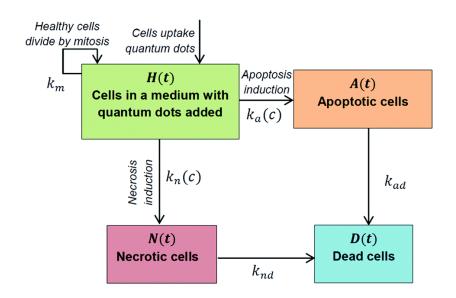
- Four states: healthy, apoptotic, necrotic, dead.
- Healthy cells can enter apoptosis or necrosis.
- Cells in apoptosis or necrosis can die.
- No reversibility.
- Rate at which cells leave healthy state depends on QD concentration.

**Uptake model:** saturation concentration  $c_s$  and current intracellular concentration c(t) with

$$c(t) = c_s(1 - e^{-k_c t}).$$
 (1)



### Model Schematic



## Model Equations

Assuming  $k_a(c)$  and  $k_n(c)$  are linear in c we have

$$\frac{dA(t)}{dt} = k_{a1}c_s(1 - e^{-k_c t})H(t) - k_{ad}A(t),$$
 (2)

$$\frac{dN(t)}{dt} = k_{n1}c_{s}(1 - e^{-k_{c}t})H(t) - k_{nd}N(t), \tag{3}$$

$$\frac{dH(t)}{dt} = (k_m - k_{a1}c_s(1 - e^{-k_ct}) - k_{n1}c_s(1 - e^{-k_ct}))H(t), \quad (4)$$

$$\frac{dD(t)}{dt} = k_{ad}A(t) + k_{nd}N(t). \tag{5}$$

Here  $k_m$  is the rate of cell division. Initial conditions:

$$H(t = 0) = H_0, A(t = 0) = N(t = 0) = D(t = 0) = 0.$$



### **Estimation**

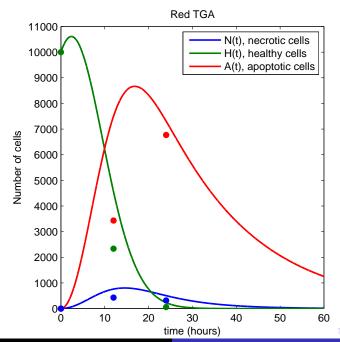
For each type of QDs, need to estimate  $k_{a1}$ ,  $k_{n1}$ ,  $c_s$ ,  $k_c$ ,  $k_{ad}$ ,  $k_{nd}$ ,  $k_m$ .

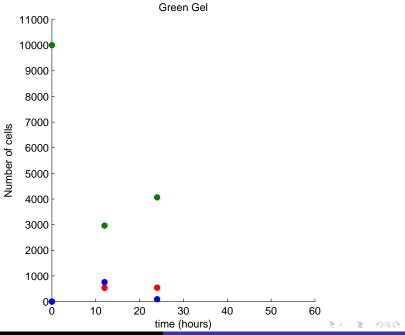
- Apoptosis takes from 6-24 hours  $\implies k_{ad} \approx 0.05 hr^{-1}$ .
- ullet Doubling time for RAW 264.7 is  $\sim$  12 hours

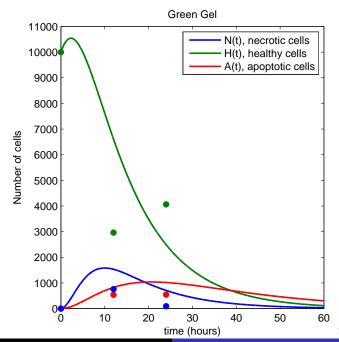
$$\implies k_m \approx \frac{\ln 2}{12} \approx 0.05 hr^{-1}$$

- Treat  $k_{a1}c_s$ ,  $k_{n1}c_s$  as single parameters (only appear as products).
- Remains to estimate  $k_{a1}c_s$ ,  $k_{n1}c_s$ ,  $k_c$ ,  $k_{nd}$  for each type.









### **Future Work**

- Need further information on uptake;
  - timescale and saturation concentration not measured;
  - differ for each type;
  - Insufficient number of time points;
- Linear assumption of transition rates probably too simple
- Stage of the cell cycle may have an effect on uptake

### References



Olga Gladkovskaya, Paul Greaney, Yurii K. Gun'ko, Gerard M. O'Connor, Martin Meere and Yury Rochev.

An experimental and theoretical assessment of quantum dot cytotoxicity.

Toxicology Research, 2015, 4, 1409-1415